

## Pre-defined

```
> DiffRing := OreTools:-SetOreRing(x,'differential');
DiffRing := UnivariateOreRing(x, differential) (1)
```

$$\begin{aligned} & \text{ShiftRing} := \text{OreTools}:\text{SetOreRing}(x, \text{'shift'}); \\ & \text{ShiftRing} := \text{UnivariateOreRing}(x, \text{shift}) \end{aligned} \quad (2)$$
$$\begin{aligned} & \text{> } QShiftRing := OreTools:-SetOreRing([x, q], 'qshift'); \\ & \quad \quad \quad QShiftRing := UnivariateOreRing(x, qshift) \end{aligned} \quad (3)$$
$$\begin{aligned} & \text{> OreTools:-Properties:-Getdelta(DiffRing)} \\ & \quad (p, var) \rightarrow \frac{\partial}{\partial var} p \end{aligned} \tag{4}$$

## User-defined

$$\begin{aligned} & \text{DeltaRing} := \text{OreTools}:-\text{SetOreRing}(x, \text{'Delta'}, \\ & \quad \text{'sigma'} = ((p, x) \rightarrow \text{eval}(p, x = x + 1)), \\ & \quad \text{'sigma\_inverse'} = ((p, x) \rightarrow \text{eval}(p, x = x - 1)), \\ & \quad \text{'delta'} = ((p, x) \rightarrow \text{eval}(p, x = x + 1) - p), \\ & \quad \text{'theta1'} = 0); \\ & \quad \text{DeltaRing} := \text{UnivariateOreRing}(x, \Delta) \end{aligned} \tag{5}$$
$$\text{OreTools}:-\text{Properties}:-\text{Getdelta}(\text{DeltaRing}) \quad (p, x) \rightarrow p \Big|_{x=x+1} - p \quad (6)$$