

> restart;

>

Load TruncatedSeries2022.zip from

http://www.ccas.ru/ca/_media/truncatedseries2022.zip

This archive includes two files: maple.ind and maple.lib.

Put these files to some directory, for example to "/usr/userlib"

> libname := "/usr/userlib", libname :

>

> with(TruncatedSeries) :

> s1 := Matrix(3, 3, [[O(x^3), O(x^3), O(x^3)], [O(x^3), K 1 + x + x^2 + O(x^3), O(x^3)], [O(x^3), K 1 + x + x^2 + O(x^3), O(x^3)]] • theta(y(x), x, 2) + Matrix(3, 3, [[1 + x + O(x^2), O(x^3), O(x^3)], [O(x^3), 2K 4*xK 4*x^2 + O(x^3), O(x^3)], [1 + x + O(x^2), 2K 4*xK 4*x^2 + O(x^3), 1 + O(x^5)]] • theta(y(x), x, 1) + Matrix(3, 3, [[K 1 + 1/2*x^2 + O(x^3), O(x^3), O(x^3)], [O(x^3), O(x^6), O(x^3)], [K 1K x + 1/2*x^2 + O(x^3), K 1 + O(x^4), O(x^3)]] • y(x);

$$s1 := \begin{bmatrix} O(x^3) & O(x^3) & O(x^3) \\ O(x^3) & K 1 + x + x^2 + O(x^3) & O(x^3) \\ O(x^3) & K 1 + x + x^2 + O(x^3) & O(x^3) \end{bmatrix} \cdot \theta(y(x), x, 2) \quad (1)$$

$$+ \begin{bmatrix} 1 + x + O(x^2) & O(x^3) & O(x^3) \\ O(x^3) & 2K 4xK 4x^2 + O(x^3) & O(x^3) \\ 1 + x + O(x^2) & 2K 4xK 4x^2 + O(x^3) & 1 + O(x^5) \end{bmatrix} \cdot \theta(y(x), x, 1)$$

$$+ \begin{bmatrix} K 1 + \frac{x^2}{2} + O(x^3) & O(x^3) & O(x^3) \\ O(x^3) & O(x^6) & O(x^3) \\ K 1K x + \frac{x^2}{2} + O(x^3) & K 1 + O(x^4) & O(x^3) \end{bmatrix} \cdot y(x)$$

> LaurentSolution(s1, y(x));

$$\left[\left[K x^2 _c_1 + x _c_1 + O(x^3), x^2 _c_2 + O(x^3), _c_3 + x^2 \left(\frac{_c_1}{2} + \frac{_c_2}{2} \right) + O(x^3) \right], \left[K x^2 _c_1 + x _c_1 + O(x^3), \right. \right. \quad (2)$$
$$\left. \left. + O(x^3), x^2 _c_2 K \frac{4x^3 _c_2}{3} + O(x^4), x^2 \left(\frac{_c_1}{2} + \frac{_c_2}{2} \right) + O(x^3) \right], \left[K x^2 _c_1 + x _c_1 + O(x^3), \right. \right.$$
$$\left. \left. O(x^3), _c_3 + \frac{x^2 _c_1}{2} + O(x^3) \right], \left[K x^2 _c_1 + x _c_1 + O(x^3), O(x^4), \frac{x^2 _c_1}{2} + O(x^3) \right], \left[x^2 _c_2 \right. \right.$$
$$\left. \left. K x _c_2 + O(x^3), x^2 _c_2 K \frac{4x^3 _c_2}{3} + O(x^4), O(x^3) \right], \left[O(x^3), x^2 _c_2 + O(x^3), _c_3 + \frac{x^2 _c_2}{2} \right. \right.$$
$$\left. \left. + O(x^3) \right], \left[O(x^3), O(x^3), _c_3 + O(x^3) \right], \left[O(x^5), x^2 _c_2 K \frac{4x^3 _c_2}{3} + O(x^5), \frac{x^2 _c_2}{2} \right. \right.$$
$$\left. \left. K \frac{4x^3 _c_2}{9} + O(x^5) \right] \right]$$

> s2 := Matrix(2, 2, [[1 + O(x^5), O(x^5)], [O(x^5), 1K x + O(x^5)]] • theta(y(x), x, 1) + Matrix(2, 2, [[O(x^5), K 1 + O(x^5)], [K x + 2*x^2 + 2*x^3 + 2*x^4 + O(x^5), K 2 + 4*x + O(x^5)]] • y(x) = 0;

(3)

$$s2 := \begin{bmatrix} 1 + O(x^5) & O(x^5) \\ O(x^5) & 1K x + O(x^5) \end{bmatrix} \cdot \theta(y(x), x, 1) \quad (3)$$

$$+ \begin{bmatrix} O(x^5) & K 1 + O(x^5) \\ K x + 2x^2 + 2x^3 + 2x^4 + O(x^5) & K 2 + 4x + O(x^5) \end{bmatrix} \cdot y(x) = 0$$

> *LaurentSolution*(s2, y(x));

$$[[K x^3 _c2 + x^2 _c2 + O(x^7), K 3x^3 _c2 + 2x^2 _c2 + O(x^7)], [K x^3 _c2 + x^2 _c2 K x _c1 + _c1 + O(x^5), K 3x^3 _c2 + 2x^2 _c2 K x _c1 + O(x^5)]] \quad (4)$$

> s3 := *Matrix*(2, 2, [[x + O(x^3), O(x^3)], [1 + O(x^3), x + O(x^3)]]).theta(y(x), x, 1) + *Matrix*(2, 2, [[O(x^3), O(x^3)], [O(x^3), 3*x + O(x^3)]]).y(x);

$$s3 := \begin{bmatrix} x + O(x^3) & O(x^3) \\ 1 + O(x^3) & x + O(x^3) \end{bmatrix} \cdot \theta(y(x), x, 1) + \begin{bmatrix} O(x^3) & O(x^3) \\ O(x^3) & 3x + O(x^3) \end{bmatrix} \cdot y(x) \quad (5)$$

By the last version, the procedure can search for Laurent solutions:

> *LaurentSolution*(s3, y(x));

$$[[_c1 + O(x^2), O(x)]] \quad (6)$$