

> restart;

- Load from [http://www.ccas.ru/ca/\\_media/truncatedseries2020.zip](http://www.ccas.ru/ca/_media/truncatedseries2020.zip) the archive with two files: maple.ind and maple.lib.

- Put these files to some directory, for example to "/usr/userlib".

- Assign libname := "/usr/userlib", libname in the Maple session.

> libname := "maple.lib", libname :

> with(TruncatedSeries);

[FormalSolution, LaurentSolution, RegularSolution]

(1)

> eq1 :=  $O(x^5) \frac{d^4}{dx^4} y(x) + (x^4 + O(x^5)) \frac{d^3}{dx^3} y(x) + O(x^3) \frac{d^2}{dx^2} y(x) + (x + O(x^2)) \frac{d}{dx} y(x) + (1 + O(x^2)) y(x) :$   
FormalSolution(eq1, y(x));

$$\left[ \frac{-c_1 + O(x)}{x} + y_{irr,1}(x) + y_{irr,2}(x) \right]$$

(2)

> eq2 :=  $(x^4 + O(x^5)) \frac{d^3}{dx^3} y(x) + O(x^3) \frac{d^2}{dx^2} y(x) + (x + O(x^2)) \frac{d}{dx} y(x) + (1 + O(x^2)) y(x) = 0 :$

> FormalSolution(eq2, y(x));

$$\left[ \frac{-c_1 + O(x)}{x} + e^{-\frac{2 \operatorname{RootOf}(-Z^2 + 1, \text{index} = 1)}{\sqrt{x}}} y_{reg,1}(\sqrt{x}) + e^{-\frac{2 \operatorname{RootOf}(-Z^2 + 1, \text{index} = 2)}{\sqrt{x}}} y_{reg,2}(\sqrt{x}) \right]$$

(3)

> eq3 :=  $(x^8 + O(x^9)) \frac{d^3}{dx^3} z(x) + O(x^5) \frac{d^2}{dx^2} z(x) + (3x^2 + O(x^3)) \frac{d}{dx} z(x) + (2 + O(x^2)) z(x) = 0 :$

> FormalSolution(eq3, z(x));

$$\left[ e^{\frac{2}{3x}} z_{reg}(x) + z_{irr(2),1}(x) + z_{irr(2),2}(x) \right]$$

(4)

> eq4 :=  $(-64x^6 + 240x^7 + O(x^8)) \frac{d^4}{dx^4} y(x) + (-512x^5 + 1680x^6 + O(x^7)) \frac{d^3}{dx^3} y(x) + (32x^3 - 888x^4 + 1980x^5 + O(x^6)) \frac{d^2}{dx^2} y(x) + (32x^2 + 60x^3 - 180x^4 + O(x^5)) \frac{d}{dx} y(x) + (-4 + 43x - 150x^2 + 180x^3 + O(x^4)) y(x) = 0 :$

> FormalSolution(eq4, y(x));

$$\left[ e^{-\frac{1}{\sqrt{x}}} (x(-c_1 + O(x)) + y_{reg,1}(\sqrt{x})) + e^{\frac{1}{\sqrt{x}}} (x(-c_2 + O(x)) + y_{reg,2}(\sqrt{x})) \right]$$

(5)

> eq5 :=  $(x^6 + O(x^7)) \frac{d^3}{dx^3} y(x) + (x^4 + O(x^5)) \frac{d^2}{dx^2} y(x) + O(x^2) \frac{d}{dx} y(x) + (x + O(x^2)) y(x) = 0 :$

> FormalSolution(eq5, y(x));

$$[y_1(x) + y_{irr}(x) + y_{irr(1)}(x)]$$

(6)